

Please show **all** your work! Answers without supporting work will not be given credit.

Name: _____

1. Logistics

- Office Hours: MS 3957, Tuesday at 10a and Thursdays at 11a
- SMC: MS 3974 Monday-Thursday 9a-3p (I'll be there Thursdays at 10a)

2. Plug and Play

Using your differentiation skills, decide which of the following (possibly more than one) are solutions to the differential equation given:

(a) $\frac{dy}{dt} = ty$

i. $y = e^{2t}$

ii. $y = e^{t^2}$

iii. $y = e^{\frac{t^2}{2}} + \pi$

iv. $y = \pi e^{\frac{t^2}{2}}$

(b) $f'(x) = f''(x) + x$

i. $f(x) = x^2/2 + x$

ii. $f(x) = e^x$

iii. $f(x) = 10$

iv. $f(x) = e^x + 10 + x^2/2 + x$

3. Come Out and Play (Keep 'em Separated)

One nice class of differential equations are the separable ones, i.e. the ones where you can move all the y stuff to one side and all the t stuff to other side. For example, with $\frac{dy}{dt} = \frac{y}{t}$, we can separate this into $\frac{dy}{y} = \frac{dt}{t}$ by multiplying both sides by dt ¹ and dividing both sides by y . If your differential equation is in Newton notation like $f'(x) = f(x)x$ it's useful to convert it to Leibniz notation $\frac{df}{dx} = f(x)x$ so you can separate it as $\frac{df}{f(x)} = xdx$. Once separated, integrate both sides.

Use separation of variables to solve the following:

(a) $\frac{dy}{dt} = \frac{y}{t}$

(b) $\frac{df}{dx} = f(x)x$

(c) $\frac{dy}{dt} = \frac{t^2 + e^t}{y}$

¹We won't be too worried about whether we can do this; for now, think of this as a mnemonic aid.

