- (Q-1) (a) Prove that any two successive Fibonacci numbers F_n, F_{n+1}, n > 0, are relatively prime.
 (b) Given that T₁ = 2 and T_{n+1} = T_n² T_n + 1, n > 0, prove that T_n and T_m are relatively prime whenever n ≠ m.
- (Q-2) Prove (a+b)/(c+d) is irreducible if ad bc = 1.
- (Q-3) Prove that $gcd(a_1, \ldots, a_m) gcd(b_1, \ldots, b_n) = gcd(a_1b_1, \ldots, a_mb_n)$, where the parentheses on the right include all mn products a_ib_j , $i = 1, \ldots, m$, $j = 1, \ldots, n$.
- (Q-4) When Mr. Smith cashed a check for x dollars and y cents, he received instead y dollars and x cents, and found that he had two cents more than twice the proper amount. For how much was the check written?
- (Q-5) Prove that any subset of 55 numbers chosen from the set {1, 2, ..., 100} must contain numbers differing by 10, 12, and 13, but need not contain a pair differing by 11.
- (Q-6) Show that $4^{3x+1} + 2^{3x+1} + 1$ is divisible by 7.
- (Q-7) (a) Prove that the sequence (in base-10 notation)

11, 111, 1111, 11111, ...

contains no squares.

(b) Prove that the difference of the squares of any two odd numbers is divisible by 8.

- (Q-8) Prove that (21n 3)/4 and (15n + 2)/4 cannot both be integers for the same positive integer n.
- (Q-9) Complete the proof of Larson 3.2.10. ("A lattice point $(x, y) \in \mathbb{Z}^2$ is visible if gcd(x, y) = 1. Prove or disprove: Given a positive integer n, there exists a lattice point (a, b) whose distance from every visible point is $\geq n$.")
- (Q-10) Prove that there does not exist an integer which is doubled when the initial digit is transferred to the end.