## MATH 10B, SPRING 2017, QUIZ 8

(1) Suppose you roll a die 100 times and 30 of the rolls are fives. Find a $95 \%$ confidence interval for the probability $p$ of rolling a five.
(2) Suppose you want to check if two random variables, $X$ and $Y$, are independent. Assume that both $X$ and $Y$ both take only the values 0 and 1. You collect some data and compile the following table of observations, which records how many times each possible outcome occurred.

|  | $\mathrm{X}=0$ | $\mathrm{X}=1$ |
| :---: | :---: | :---: |
| $\mathrm{Y}=0$ | 300 | 100 |
| $\mathrm{Y}=1$ | 200 | 400 |

(a) Fill in the following table of expected frequencies (i.e. assuming the null hypothesis that the two variables are independent). You do not need to simplify your answers.

|  | $\mathrm{X}=0$ | $\mathrm{X}=1$ |
| :--- | :--- | :--- |
| $\mathrm{Y}=0$ |  |  |
| $\mathrm{Y}=1$ |  |  |

(b) Calculate the $\chi^{2}$ statistic for the given data. You do not need to simplify your answer.
(c) What is the number of degrees of freedom for the $\chi^{2}$ test on the given data?

