

Math 3B: Lecture 18

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November 13, 2017

Checking solutions

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$$\begin{aligned}\frac{dy}{dx} &= e^{\sin x} \cos x \\ y \cos x &= e^{\sin x} \cos x\end{aligned}$$

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4. solve for y !

Examples

On the board. . .