

ORAL FINAL EXAM REVIEW

THEOREMS & RESULTS YOU HAVE TO KNOW

- (1) The 3 Isomorphism Theorems
- (2) The universal property of the quotient (explain how to construct the map from the quotient and why it gives a bijection between the relevant sets)
- (3) The universal property of the tensor product (explain how to construct maps from the tensor product and why it gives an identification with bilinear maps)
- (4) Riesz representation theorem for a non-degenerate bilinear form
- (5) The theorem about cyclic subspaces for nilpotent spaces (the one that requires the top non-zero powers of a linear operator on the set be linearly independent).
- (6) Choice of a basis gives an isomorphism with a free vector space. Choice of an orthonormal basis gives an isomorphism with $\mathbb{R}^n$ or $\mathbb{C}^n$ with the dot product.
- (7) The dual of a short exact sequence is short exact

THINGS YOU MUST BE ABLE TO COMPUTE

- (1) Jordan form and Jordan basis
- (2) Gram-Schmidt orthogonalization
- (3) The value of the exterior powers of a linear operator on various elements

That's it!