Quiz the Last

1. Find the third order Fourier approximation to f(x) = 3x.

2. Convert $\{1,x\}$ into an orthogonal set with respect to the inner product $\langle f,g\rangle=\int_0^2 f(x)g(x)dx.$

3. Let $L: P_2(x) \to P_1(x)$ be given by L(p) = p' + 2p''. Let $\mathcal{B} = \{1, x, x^2\}$ be a basis for P_2 , and let $\mathcal{B}' = \{1, x + 1\}$ be a basis for P_1 . Find the matrix representation of L with respect to \mathcal{B} and $\mathcal{B}': _{\mathcal{B}'}[L]_{\mathcal{B}}$.