Problem 1.
Suppose the rectangle has dimensions $n, m$. Then its area is $nm$. Since both $n$ and $m$ are integers, they are positive divisors of 31. But 31 is prime, so one of $n, m$ must be 1 and the other 31. Then the perimeter is $2n + 2m = 64$. 