Warm-up problems

1. A squad of six soldiers must cross a deep river with no bridge. They spot two children playing with a small boat by the shore. The boat can only hold two children or one soldier. Can all the soldiers make it across the river?

2. In a ten-story building, only one person lives on the first floor; two people live on the second floor; three people live on the third floor, and so on up to the tenth floor where ten people live. On which floor does the elevator stop the most?
1. Suppose you are cutting a log by using a hand saw.

- How many pieces will you get if you cut a log with 3 cuts?

   Answer: You get \[ \boxed{4} \] pieces.

- What about 10 cuts?

   Answer: You get \[ \boxed{11} \] pieces.

- What about 27 cuts?

   Answer: You get \[ \boxed{28} \] pieces.

- What about 2017 cuts?

   Answer: You get \[ \boxed{2018} \] pieces.
How is the number of pieces related to the number of cuts?

Do you notice a pattern?

\[ \text{PIECES} = \text{CUTS} + \square \]

Can you explain this?
2. How many cuts do you have to make to cut a log into 3 pieces?

- What about 10 pieces?

- What is the general rule here?

\[
CUTS = PIECES \square 1
\]
3. Now suppose that you have 2 logs. Use 4 cuts to get some number of pieces. It is your choice how many cuts to make on each log, but the total must be 4.

(a) how many pieces do you get?

First attempt:

Answer: you get [ ] pieces.

Second attempt:

Answer: you get [ ] pieces.

(b) Did you get the same number of pieces each time? Can you explain this?
4. You still have 2 logs and make some cuts on both of them. The total number of cuts is 10. How many pieces do you get?

Use the space below to make pictures that can help you:

Answer: When you make 10 cuts on 2 logs you get \[
\]
pieces.
5. Suppose you have 2 logs. How is the number of pieces related to the total number of cuts you make?

\[ \text{PIECES} = \text{CUTS} + \square. \]

6. What happens when you cut 3 logs? Investigate this idea, and see what general pattern you can find. \[ \text{PIECES} = \text{CUTS} + \square. \]
7. The Tin Man says that he got 10 pieces after making just five cuts. How many logs did he start with?

8. The Tin Man says that he can also get 10 pieces of wood by making only three cuts. Do you believe him? If yes, how can he do it? If no, why not?
9. Now you have a bagel instead of a log. We will be cutting it in a funny way. A cut goes from the hole to the edge of the bagel. Thus, one cut DOES NOT create two pieces.) Make a picture.

- If you cut a bagle with 3 cuts, how many pieces do you get?

- How many pieces will you get if you cut a bagel with 5 cuts?

What about 10 cuts?

What happens if you make just one cut? What is the general rule here? Does it work for any number of cuts?
10. Suppose you have 2 bagels. You cut each bagel some number of times so that all together there are 4 cuts. How many pieces do you get? Does it depend on how many cuts you choose to put on each log?

11. What happens if you take two bagels and make a total of 7 cuts on them. How many pieces can you get? Can you come up with a general rule for the number of pieces you can get by cutting two bagels?
12. Now suppose you have 3 bagels and you make 3 cuts. How many pieces can you get?

13. Dorothy says she got 4 bagel slices after making 3 cuts. Find out how many bagels she could have started with.