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Uniform finiteness and infinite discrete sets

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Recall that a theory T is said to satisfy uniform finiteness if for any uniformly definable family of sets there is a natural number N so that any finite set in the family has cardinality at most N . Let T be an expansion of the theory of dense linear orderings. If T does not satisfy uniform finiteness then in some model of T there is an infinite definable discrete set. We consider consequences of this fact and investigate when the converse holds and examples where it does not.