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**Conservative pairs of models in weakly o-minimal theories**

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It is said that a pair of models  $(M, N)$  is conservative pair, if for any finite tuple of elements of  $N$ , its type over  $M$  is definable. We say that  $N$  is CD- $\omega$ -saturated if any non isolated one-type over  $M$  and tuple elements from  $N$ , which is determined by its restriction to some definable  $\phi$ -type, is realized in  $N$ . We prove that any model of any weakly o-minimal theory (except o-minimal expansions of models of the theory of discrete order with endpoints) has a conservative extension and more, has CD- $\omega$ -saturated conservative extension. The existence of conservative and CD- $\omega$ -saturated conservative extensions for o-minimal models had been proved accordingly by D. Marker and Baisalov-Poizat. We consider the cases for weakly o-minimal theories, when the class of of CD- $\omega$ -saturated conservative pairs is axiomatizable. A .Pillay proved the axiomatisability of such class for arbitrary o-minimal theory.