

Math 191, Networks, UCLA, Spring 2018  
*Quiz 1*

1. Consider an unweighted, undirected, simple network.
  - a. Show that the smallest eigenvalue of the combinatorial graph Laplacian  $\mathbf{L} = \mathbf{D} - \mathbf{A}$  is 0.
  - b. Show that the number of components in the network is equal to the number of 0 eigenvalues of  $\mathbf{L}$ .