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## First computational project: due no later than May 10, 2010

(i) Show that the problem

$$\begin{cases} -u''(x) + u(x) = f(x), & 0 < x < 1, \\ u(0) = 0, & u'(1) = 0 \end{cases}$$

can be given a weak variational formulation.

- (ii) Formulate a FEM for this problem using piecewise-linear functions. Determine the corresponding linear system of equations in the case of a uniform partition and study in particular how the boundary condition u'(1) = 0 is approximated by the method.
- (iii) Write a computer program for the piecewise-linear FEM applied to this problem. Present calculations with h=0.1 and h=0.2, for  $f(x)=2+2x-x^2$ . Approximate  $\int f(x)\varphi_j(x)dx$  by a quadrature formula of your choice. The exact solution of the problem is u(x)=x(2-x).

(see section 1.8: Remarks on programming)