269C, Spring 2006, Vese

First computational project: Due on Friday, May 19

Show that the problem

$$\begin{cases} -u''(x) + u(x) = f(x), & 0 < x < 1, \\ u(0) = 0, & u'(1) = 0 \end{cases}$$

can be given a weak variational formulation.

Formulate a FEM for this problem using piecewise-linear functions. Determine the corresponding linear system of equations in the case of a uniform partition and study in particular how the boundary condition u'(1) = 0 is approximated by the method.

Write a computer program for the piecewise-linear FEM applied to this problem. Present calculations with h = 0.1 and h = 0.2, for $f(x) = 2 + 2x - x^2$. Approximate $\int f(x)\varphi_j(x)dx$ by a quadrature formula of your choice. The exact solution of the problem is u(x) = x(2-x).

(see also section 1.8: Remarks on programming)