

We know that  $q_1 = (1 \ 0 \ 2 \ -1)$   
 $q_2^T = (0 \ 1 \ -1 \ 0)$   
 ~~$q_3^T = (0 \ 0 \ 1 \ 2)$~~  are active at  
 $q_5^T = (-3 \ 0 \ 0 \ 1)$   $(1, 1, 1, 2)^T$

In order that  $p = (-1 \ 1 \ 1 \ a)$  to be a feasible direction we have

$$q_1^T p \geq 0 \text{ which implies } (1 \ 0 \ 2 \ -1) \begin{pmatrix} -1 \\ 1 \\ 1 \\ a \end{pmatrix} = 1 - a \geq 0 \\ \Rightarrow \boxed{a \leq 1}$$

$$q_2^T p \geq 0 \text{ which implies } (0 \ 1 \ -1 \ 0) \begin{pmatrix} -1 \\ 1 \\ 1 \\ a \end{pmatrix} = 1 > 0$$

$$q_5^T p \geq 0 \text{ which implies } (-3 \ 0 \ 0 \ 1) \begin{pmatrix} -1 \\ 1 \\ 1 \\ a \end{pmatrix} = 3 + a \geq 0 \\ \Rightarrow \boxed{a \geq -3}$$

$$\text{So } \boxed{-3 \leq a \leq 1}$$