

Math 155, Vese

Homework # 3 Due on Wednesday, May 12

[1] Show that the Fourier transform and its inverse are linear processes.

[2] Compute in continuous variables the Fourier transform of the function defined by:

$$f(x) = \begin{cases} A, & \text{if } 0 \leq x \leq K, \\ 0, & \text{otherwise,} \end{cases}$$

where A and K are positive constants. Evaluate $F(0)$.

[3] Show that if a filter transfer function is real and symmetric (i.e. if $H(u, v) = \overline{H(u, v)} = \overline{H(-u, -v)} = H(-u, -v)$), then the corresponding spatial domain filter $h(x, y)$ is also real and symmetric.

[4]

(a) Implement the Gaussian lowpass filter in Eq. (4.3-8), using a radius=15, and apply the algorithm to the attached image.

(b) Highpass the input image used in (a), using a highpass Gaussian filter of radius $D_0 = 15$.