

**Math 151A**

**HW #1, due on Friday, April 13**

[1] Using four-digit rounding arithmetic and rationalizing the numerator, find the most accurate approximations to the roots of the following quadratic equation. Compute the absolute errors and the relative errors.

$$\frac{1}{3}x^2 - \frac{123}{4}x + \frac{1}{6} = 0.$$

[2]

(a) Show that the polynomial nesting technique described in Section 1.2 can also be applied to the evaluation of

$$f(x) = 1.01e^{4x} - 4.62e^{3x} - 3.11e^{2x} + 12.2e^x - 1.99.$$

(b) Use three-digit rounding arithmetic, the assumption that  $e^{1.53} = 4.62$ , and the fact that  $e^{nx} = (e^x)^n$  to evaluate  $f(1.53)$  as given in part (a).

(c) Redo the calculation in part (b) by first nesting the calculations.

(d) Compare the approximations in parts (b) and (c) to the true three-digit result  $f(1.53) = -7.61$ .

You can use a hand calculator or the Bisection Algorithm posted on the class webpage.

[3] Use the Bisection method to find  $p_3$  for  $f(x) = \sqrt{x} - \cos x$  on  $[0, 1]$ .

[4] Find an approximation to  $\sqrt{3}$  correct to within  $10^{-4}$  using the Bisection Algorithm (hint: consider  $f(x) = x^2 - 3$ ).

[5] Find a bound for the number of iterations needed to achieve an approximation with accuracy  $10^{-4}$  to the solution of  $x^3 - x - 1 = 0$  lying in the interval  $[1, 2]$ . Find an approximation to the root with this degree of accuracy.