

**Math 266B Winter 2013: Homework 8. Due 3/15 in class.**

1-3. Evans p. 165. Problem 17,19,20.

4. [Finite propagation property] Let  $u$  be a nonnegative solution of the porous medium equation

$$(PME_m) \quad u_t - \Delta(u^m), \quad m > 1$$

such that  $u$  is smooth in  $\{u > 0\}$ .

- (a) Let us assume that  $v = \frac{m}{m-1}u^{m-1}$  is differentiable in  $\overline{\{v > 0\}} = \overline{\{u > 0\}}$ . Verify that for  $u$  as the Barenblatt solutions (given in (35)-(36) in p186 Evans) the assumption holds.
- (b) Show that, for any point  $(x, t) \in \partial\{u > 0\}$  with  $t > 0$ , the outward normal velocity of the set  $\{u(\cdot, t) > 0\}$  at  $x$  is given by  $|Dv|(x, t)$  (Hint: compute the PDE that  $v$  satisfies)