

**Errata** as of September 16, 2011  
**Geometric Modular Forms and Elliptic Curves, First edition**  
 World Scientific Publishing Company, Singapore, 2000

Here is a table of misprints in the above book (most of them already corrected in the more recent version of the first edition), and “P.3 L.5b” indicates fifth line from the bottom of the page three. Some of them is corrected in 2005 when reprinted.

page and line	Read	Should Read
P.13 L.10	$A_k A_l = A_{k+l}$	$A_k A_l \subseteq A_{k+l}$
P.15 L.3b	$\frac{ya^{ej}}{a^k/b^{dj}}$	$\frac{ya^{ej}}{a^k b^{dj}}$
P.20 L.8	$x_n \in A$	$x^n \in A$
P.25 L.16b	there exist	there exists
P.27 L.11b	the coimage	the coimage $L$
P.30 L.14	$ab\delta(c) = \phi(b, c)$	$ab\delta(c) = a\phi(b, c)$
P.35 L.12b	open subschemes in $S$	open subschemes $U$ in $S$
P.35 L.8b	$f : \text{Spec}_S(R) \rightarrow S$	$\text{Spec}_S(R) \rightarrow S$
P.41 L.1	$SCH$	$AFF$
P.44 L.14	covariant functor	morphism of covariant functors
P.57 L.4b	an $Y$ -scheme	a $Y$ -scheme
P.78 L.2b	$g = f \times \text{id}_Y : X' \rightarrow Y$	$g = f \times \text{id}_Y : X' \rightarrow Y'$
P.83 L.6b	$(M \otimes_A R \otimes_R R) \otimes_A R$	$(M \otimes_A R \otimes_R R) \otimes_A R$
P.86 L.8	$X' \times_S T \cong T \times_S X'$	$X' \times_S T' \cong T' \times_S X'$
P.87 L.12b	$T \times_S T \times_T X$	$T \times_S T \times_T X'$
P.106 L.6	$\deg(D) \geq 2g + 1$ . Then	$\deg(D) \geq 2g + 1$ , then
P.109 L.5b	automorphism	endomorphism
P.112 L.11b	2 at 0	2 at $\mathbf{0}$
P.117 L.5b	$Y^2 Z^3$	$Y^2 Z$
P.120 (G0)	$\lambda^{-k} f((E, \omega)_R)$	$\lambda^{-k} \phi((E, \omega)_R)$
P.129 L.9	$\text{Proj}\left(\frac{\mathbb{Z}[\frac{1}{6}][[q]][X, Y, Z]}{(Y^2 - 4X^3 + g_2(q)X + g_3(q))}\right)$	$\text{Proj}\left(\frac{\mathbb{Z}[\frac{1}{6}][[q]][X, Y, Z]}{(Y^2 Z - 4X^3 + g_2(q)XZ^2 + g_3(q)Z^3)}\right)$
P.129 (2.26)	$Z[1/6][[q]]$	$Z[1/6][[q]]$
P.133 L.18b	$u + tu = t^3 - b_2 u^2 t - b_3 + 3u^3$	$u + tu = t^3 - b_2 u^2 t - b_3 u^3$
P.133 L.16b	$\Omega_{\widehat{\mathcal{O}}_{E_\infty, 0}/\mathbb{Z}[[q]]} = \mathbb{Z}[[q, u]]du$	$\Omega_{\widehat{\mathcal{O}}_{E_\infty, 0}/\mathbb{Z}[[q]]} = \mathbb{Z}[[q, t]]dt$
P.137 L.14	$A/\mathfrak{m}_A$ Such	$A/\mathfrak{m}_A$ . Such (insert a period).
P.140 L.13–14	$\mathbb{Z}[[q_N]]$	$\mathcal{O}[[q_N]]$
P.144 L.5b	$D = (\mathcal{L}', \ell')$	$D' = (\mathcal{L}', \ell')$
P.144 L.4b	$\phi^*(\mathcal{L} \otimes \mathcal{O}_D)$	$\phi^*(\mathcal{L} \otimes \mathcal{O}_{D'})$
P.145 L.14	corresponds a unique	corresponds to a unique
P.146 L.5b	(see Propositions 1.8.2 and 1.8.1)	(see Theorem 1.8.2 and Proposition 1.8.1)
P.148 L.9b	(1) $N$ is	(1) If $N$ is
P.154 L.12	$M_3$	$M_{3N}$
P.155 L.16b, 15b	$\mathcal{M}_N$	$M_N$
P.156 L.4b	components. By	components. Put $\overline{M}_N = \text{Proj}(G_N)$ . By
P.163 L.15	$\ell \nmid Np$	$p \nmid N\ell$
P.163 L.11b	$\det(1 - \rho_\ell(Frob_p) _V)$	$\det(1 - \rho_\ell(Frob_p) _V X)$
P.165 L.3	$H^0(I_p, T_\ell E) = 0$	$H_0(I_p, T_\ell E) = 0$
P.174 L.17	$\phi_p^{et} : (\mathbb{Z}/p^r\mathbb{Z})/C$	$\phi_p^{et} : (\mathbb{Z}/p^r\mathbb{Z})^2/C$
P.175 L.7	$E_{\mathfrak{a}}/E[p^r]$	$E_{\mathfrak{a}}/E_{\mathfrak{a}}[p^r]$
P.177 L.5b	object, $A$	object $A$
P.179 L.9b, 7b	$(E, \phi_N, \omega)$	$(\mathcal{E}, \phi_N, \omega)$
P.179 L.6b, 5b	$\varphi(E)$	$\varphi^*(E)$
P.182 L.8b	upper unipotent	upper triangular
P.188 L.15	$pR = 0$	$p(R/\mathfrak{a}) = 0$

page and line	Read	Should Read
P.190 L.5b	(Exercise 3).	(Exercise 4).
P.191 L.17	$\text{Gal}(\overline{\mathbb{Q}}, \mathbb{Q})$	$\text{Gal}(\overline{\mathbb{Q}}/\mathbb{Q})$
P.198 L.11	an $A$ -algebra $R$ ,	the $A$ -algebra $R$ ,
P.199 L.10b	$H^0(G, p^{-1}(U))$	$H^0(G, \underline{\omega}(p^{-1}(U)))$
P.200 L.13b	(see Remark 1.8.4 (2))	(see Proposition 1.8.4 (2))
P.203 L.8	$X_0(N)$ . The	$X_0(N)$ , the
P.203 L.28	$f \in S_k(-)$	$f \in G_k(-)$
P.207 L.6	$H^0(X, -)$	$H^1(X, -)$
P.207 L4b.	$\chi \pmod{\mathfrak{m}_A}$ of $A$	$\chi \pmod{\mathfrak{m}_A}$
P.210 L.3b	$\text{Proj}(G_{\Gamma_1(N)}(A))$	$\text{Proj}(G_{\Gamma_1(N)}(A))$
P.213 L.7	$q$ -expansions	$q$ -expansion
P.216 L.15	$O_p/p^r O_p$	$O_p/p^n O_p$
P.218 L.7	$P_m \otimes_{\mathbb{Z}/p^n \mathbb{Z}} \mathcal{O}_{T_{m,n}}$	$P_m \otimes_{\mathbb{Z}/p^m \mathbb{Z}} \mathcal{O}_{T_{m,n}}$
P.219 L.5b	$V_{m,m}$	$V_{m,\infty}$
P.220 L.8	when $S_m$ is affine	when $S$ is affine
P.225 L.4b	$r_n$	$r_m$
P.226 L.12	Since $eE^k f_i$ is	Since $E^k f_i$ is
P.227 L.3b	$M_{\Gamma, \alpha}^{\text{ord}} / (\mathbb{Z}/p^m \mathbb{Z})$	$\overline{M}_{\Gamma, \alpha}^{\text{ord}} / (\mathbb{Z}/p^m \mathbb{Z})$
P.228 (3.26)	$\text{Hom}_{p-\text{ALG}}(V_\Gamma, A)$	$\text{Hom}_{p-\text{ALG}}(V_\Gamma, [\frac{1}{\Delta}], A)$
P.230 ( $G_p$ 3), ( $S_p$ 3)	Replace $f(E_{0,N}, \phi_p^{\text{can}}, \phi_N)$ by $f(E_{0,N}, z\phi_p^{\text{can}}, \phi_N)$ and add “for all $z \in \mathbb{Z}_p^\times$ ”.	rank $p^\alpha$
P.234 L.12	rank $p^r$	$f  \langle d \rangle$
P.236 (3.34)	$f  \langle a \rangle$	$G'_\Gamma(A[1/p])$
P.236 L.17	$G'_\Gamma(A[1/p])$	(resp. a ring)
P.237 L.14	(a ring)	the cusp of the Tate curve
P.238 L.11b	the Tate curve	diamond operators $\langle z \rangle$
P.238 L.9b	diamond operators	$z \in \mathbf{G}_m(\mathbb{Z}_p) = \mathbb{Z}_p^\times$
P.238 L.8b	$\mathbf{G}_m(\mathbb{Z}_p) = \mathbb{Z}_p^\times$	between
P.239 L.11b	of between	subgroup $\Gamma_Z$
P.244 L.11b	subgroup $\Gamma_T$	
P.260 L.1-2	See Addenda below	
P.260 L.3	$\sum_k n_k j_k = r$	$\sum_k j_k = r$
P.264 L.17b	(Corollary 2.1.7)	(Corollary 2.1.5)
P.265 L.17	$\mathcal{L}$ on $C_j$	$\mathcal{L}$ on $C$
P.266 L.10b	fiber a union	fiber a smooth curve or a union
P.268 L.9	Obviously.	Obviously,
P.279 L.15b	$X \times_S X \cong \text{Ker}(f) \times_S Y$	$X \times_Y X \cong \text{Ker}(f) \times_S Y$
P.285 L.2b	rank $_{\mathbb{Z}} O_s$	rank $_{\mathbb{Z}_p} O_s$
P.293 L.16	cyclic subgroup $C$ of order $p$	locally free subgroup $C$ of rank $p$
P.293 L.19	$\phi'_N \circ \pi = \phi_N$	$\phi'_N = \pi \circ \phi_N$
P.295 L.4	$T^2 - T(p)X + p\langle p \rangle = 0$	$X^2 - T(p)X + p\langle p \rangle = 0$
P.295 L.11	which are to	which are
P.301 L.6b	Theorem 2.9.13 (1)	Theorem 2.9.13 (3)
P.309 L.17	diagonal	upper-triangular
P.309 L.11b	$\mathbb{Q}_p(\lambda)$	$\mathbb{Q}_\ell(\lambda)$
P.311 L.8	$\varepsilon_\alpha(p) = p^2 \omega(p)^{-2} \varepsilon_\alpha(p)$	$\varepsilon_\alpha(p) = p^2 \omega(p)^{-2} \varepsilon(p)$
P.324 Th.5.1.4	$m\sigma_1 + n\sigma_2$	$-m\sigma_1 - n\sigma_2$
P.326 L.4b	has proved	have proved
P.329 L.18	$I/I_p$	$I/I_1$
P.345 L.11, 12	$M_5 \times_{\mathbb{Q}} \mathbb{Q}(E[5])$	$M_{\Gamma(5)} \times_{\mathbb{Q}(\mu_5)} \mathbb{Q}(E[5])$
P.345 L.3b	$p \neq 5..$	$p \neq 5.$
P.347 L.8b	Topologis	Topologie

page and line	Read	Should Read
P.349 L.3b	ellitpiques,	elliptiques,
P.352 L.1	[Ri4] Report	[Ri4] K. A. Ribet, Report
P.357 (W1-3)	(W1-3), 309	(W1-3), 310
P.359 L9-10		Add “diamond operator, 235”

## Addenda

- Page 243 Line 17-14 from bottom: Replace the sentence starting from “Since on  $\mathbf{G}_{\Gamma,\Lambda}$ ,” ending “weight  $s$ .” by the following: “The map is injective by the  $q$ -expansion principle (Corollary 3.2.11). Since on  $\mathbf{G}_{\Gamma,\Lambda}$ , the two  $\Lambda$ -module structures coincide, this map brings  $\Phi \in \mathbf{G}_{\Gamma,\Lambda}$  to a  $p$ -adic modular form of weight  $s$ .”
- Page 260 Lines 1: Add the following after “we have”: “supposing the divisor  $P$  has  $s$  distinct points of  $C$  with multiplicities  $j_1, j_2, \dots, j_s$ ,”
- Page 260 Line 2: Replace the formula by the following:

$$\widehat{\mathcal{O}}_{C^r, \pi^{-1}(P)} \cong R[[T_1, \dots, T_r]]^n \quad (n = r! / j_1! j_2! \cdots j_s!)$$