

(801, #33) The radius of a right circular cylinder is decreasing at a rate of 1.2 cm/s while its height is increasing at a rate of 3 cm/s. At what rate is the volume of the cylinder changing when the radius is 80 cm and the height is 150 cm?

Solution: Since the volume of the cylinder is $V = \pi r^2 h$ we have

$$\frac{dV}{dt} = \pi \left(2rh \frac{dr}{dt} + r^2 \frac{dh}{dt} \right) = \pi r(2h(-1.2) + r(3))$$

When $r = 80$ and $h = 150$ we have

$$\frac{dV}{dt} = \pi 80^2 (-2.4 + 3) = 96 \cdot 10^2 \pi$$