

Assignment #4

Extra office hour: Tuesday, October 26, 1-2.

Problems due in lecture on **Wednesday**, October 27:

| § | page | NTHI | THI |
|------|--------|--------------------------------------|--------------------------------|
| §3.6 | p. 139 | 6(c,d), 10(c) | 8, 18(a) |
| §4.1 | p. 157 | 1(all, any method), 3(b,c), 4(a,d,m) | 2(a,e,h), 3(f,g,h), 4(b,f,g,p) |

Also to hand in:

Problem K-1. Prove that the derivative of x^n is nx^{n-1} (for $n = 1, 2, \dots$) by a direct proof rather than by induction. Use the binomial theorem.

(The direct proof for $n = 2$, for example, would be that if $f(x) = x^2$ then

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \rightarrow 0} \frac{(x+h)^2 - x^2}{h} = \dots = \lim_{h \rightarrow 0} (2x+h) = 2x.$$

Of course, x is treated as a constant while you're taking the limit $h \rightarrow 0$. For this problem, you'll need to fill in the missing steps and do this for n in place of 2, without saying which integer n is and without assuming the case $n - 1$. Express the reasoning as best you can.)